

# Advanced Modified Time Deviation Method for Job Sequencing

R. Rajalakshmi<sup>1</sup>, S. Rekha<sup>2</sup>

<sup>1</sup> MSc Mathematics, Department of Mathematics, Dr. SNS Rajalakshmi College of Arts and Science(Autonomous), Coimbatore, Tamil Nadu, India

<sup>2</sup>Assistant Professor, Department of Mathematics, Dr. SNS Rajalakshmi College of Arts and Science(Autonomous), Coimbatore, Tamil Nadu, India

## ABSTRACT

Job sequencing is the arrangement of the task that is to be precede in a machine in that particular order. In this paper, we proposed “Advanced modified time deviation method” for solving the optimal sequence for n-jobs. This method is first used for 2-machine n-jobs problem and extended for 3-machine n-jobs problem and also extended for m-machine n-job problem, by using Johnson’s algorithm to find total elapsed time.

**Keywords :** Advanced Modified Time Deviation Method, Total Elapsed Time, Optimal Solution, Johnson’s Algorithm

## I. INTRODUCTION

Operation research can be defined as the science of decision-making. It has been successfully in providing a systematic and scientific approach to all kind of government, Military, manufacturing, and service operations. Operation research deals with the application of advanced analytical method to help make better decisions. Sequencing problem is one of the important application of OR. A sequence is the order for a series of jobs to be done on a finite number of service facilities, in some pre-assigned order, is called sequencing.

## II. PRIOR WORK

### 2.1 Jobs:

The jobs or items are used in sequencing. There should be a certain number of jobs called n-jobs to be processed or sequenced.

### 2.2 Processing time:

The time it take to compete a prescribed procedure; “they increase output by increasing processing time”. Every operation requires certain time at each of

machine. Interval during a material is changed from one to another through machines, compounding or other operations.

### 2.3 Total elapsed time:

Elapsed time is the amount of time that passes from the start of an event to its finish. This activity allows the user to practice determining the elapsed time. Elapsed time is the difference between beginning and ending time.

## III. ADVANCED MODIFIED TIME DEVIATION METHOD

This method is used to find the optimal sequence of the job. In this method time duration table is calculated for each rows and columns in a cell.

1. We can find the row deviation of the cell in the time duration table by using

(Maximum time duration of the row) – (time duration of the cell)

$$r_{ij} = p_i - t_{ij} \quad (1)$$

where,  $p_i$  – maximum time of the  $i^{\text{th}}$  row

$r_{ij}$  - row time deviation of the  $(i,j)^{\text{th}}$  cell

$t_{ij}$  – time required for processing  $i^{th}$  job on the  $j^{th}$  processing.

2. We can find the column deviation of the cell in the time duration table by  
(Maximum time duration of the column) – (time duration of the cell)

$$s_{ij} = c_i - t_{ij} \tag{2}$$

where,  $c_i$  – maximum time of the  $i^{th}$  column

$s_{ij}$  - column time deviation of the  $(i,j)^{th}$  cell

$t_{ij}$  – time required for processing  $i^{th}$  job on the  $j^{th}$  processing.

3. We can find the time duration of the cell by using

$$T_{ij} = r_{ij} + s_{ij} \tag{3}$$

**3.1 Algorithm**

1. Start
2. Read the number of jobs and processing time for each jobs on  $M_1$  &  $M_2$

3. Calculate the time duration table for the given sequencing problem
4. The cell which contains the time as zero in  $M_1$ , perform the job in first
5. If more than one cell has zero then compare the jobs in  $M_2$ , which has the smallest value consider that has the first job
6. Similarly repeat the above steps for  $M_2$  and perform the job last
7. Stop the procedure if we get the optimal sequence for all jobs
8. And use Johnson’s algorithm to find the total elapsed time.

**3.2 Numerical examples:**

**3.2.1 Sequencing n-jobs through 2-machine**

Using advanced modified time deviation method for 2-machine n-jobs problem to find optimal sequence

**Table 1**

Job Machine	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>
M <sub>1</sub>	3	5	2	6
M <sub>2</sub>	4	2	3	2

**Solution:**

**Table 2**

Job Machine	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>
M <sub>1</sub>	3	5	2	6
M <sub>2</sub>	4	2	3	2

Calculate time duration table by using advanced modified time deviation method

**Table 3**

Job Machine	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>
M <sub>1</sub>	(3+1)	(1+0)	(4+1)	(0+0)
M <sub>2</sub>	(0+0)	(2+3)	(1+1)	(2+4)

**Table 4**

Job Machine	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>
M <sub>1</sub>	4	1	5	0
M <sub>2</sub>	0	5	2	6

J <sub>4</sub>			J <sub>1</sub>
----------------	--	--	----------------

Repeat the process until get the optimal sequence for all jobs

**Table 5**

Job Machine	J <sub>2</sub>	J <sub>3</sub>
M <sub>1</sub>	5	2
M <sub>2</sub>	2	3

**Table 6**

Job Machine	J <sub>2</sub>	J <sub>3</sub>
M <sub>1</sub>	0	4
M <sub>2</sub>	4	0

The required optimal sequence is

J <sub>4</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>1</sub>
----------------	----------------	----------------	----------------

After finding the optimal sequence we have to find the total elapsed time by using Johnson’s algorithm

**Table 7**

	M <sub>1</sub>		M <sub>2</sub>	
	In time	Out time	In time	Out time
J <sub>4</sub>	0	6	6	8
J <sub>2</sub>	6	11	8	10
J <sub>3</sub>	11	13	10	13
J <sub>1</sub>	13	16	13	17

Total elapsed time is 17 hrs. Idle time of M<sub>1</sub> is 1 hr and idle time of M<sub>2</sub> is 6 hrs.

**3.2.2 Sequencing n-jobs through 3-machine**

Using advanced modified time deviation method for 3-machine n-job problem to find optimal sequence

**Table 8**

Job \ Machine	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>	J <sub>5</sub>	J <sub>6</sub>	J <sub>7</sub>
M <sub>1</sub>	3	8	7	4	9	8	7
M <sub>2</sub>	4	3	2	5	1	4	3
M <sub>3</sub>	6	7	5	11	5	6	12

**Solution:**

**Table 9**

Job \ Machine	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>	J <sub>5</sub>	J <sub>6</sub>	J <sub>7</sub>
M <sub>1</sub>	3	8	7	4	9	8	7
M <sub>2</sub>	4	3	2	5	1	4	3
M <sub>3</sub>	6	7	5	11	5	6	12

Calculating time duration table by using advanced modified time deviation method

**Table 10**

Job Machine	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>	J <sub>5</sub>	J <sub>6</sub>	J <sub>7</sub>
M <sub>1</sub>	9	1	2	12	0	1	7
M <sub>2</sub>	3	7	8	6	12	5	11
M <sub>3</sub>	6	6	9	1	11	8	0

The required optimal sequence is

J <sub>5</sub>	J <sub>7</sub>	J <sub>4</sub>	J <sub>2</sub>	J <sub>6</sub>	J <sub>3</sub>	J <sub>1</sub>
----------------	----------------	----------------	----------------	----------------	----------------	----------------

After finding the optimal sequence we have to find the total elapsed time by using Johnson’s algorithm

**Table 11**

	M <sub>1</sub>		M <sub>2</sub>		M <sub>3</sub>	
	In time	Out time	In time	Out time	In time	Out time
J <sub>5</sub>	0	9	9	10	10	15
J <sub>7</sub>	9	16	16	19	15	27
J <sub>4</sub>	16	20	20	25	27	38
J <sub>2</sub>	20	28	28	31	38	45
J <sub>6</sub>	28	36	36	40	45	51
J <sub>3</sub>	36	43	43	45	51	56
J <sub>1</sub>	43	46	46	50	56	62

Total elapsed time is 62 hrs. Idle time of M<sub>1</sub> is 16 hr and idle time of M<sub>2</sub> is 12 hrs and idle time for M<sub>3</sub> is 10 hrs.

Also we can extend this method for n-jobs 4-machine and etc till n-job m-machine.

**3.2.1 Sequencing n-jobs through m-machine**

Using advanced modified time deviation method for m-machine n-jobs problem

To sequence the m-machine n-job problem we have to convert the m-machine n-jobs problem to 2-machine n-job problem

We are introducing two machines namely G & H

- $G = (M_1 + M_2 + \dots + M_{m-1}) \geq M_m$  (4)
- $H = (M_2 + M_3 + \dots + M_m) \geq M_1$  (5)

**Table 12**

Job Machine	J <sub>1</sub>	J <sub>2</sub>	.....	J <sub>n</sub>
M <sub>1</sub>	T <sub>11</sub>	T <sub>12</sub>	.....	T <sub>1n</sub>
M <sub>2</sub>	T <sub>21</sub>	T <sub>22</sub>	.....	T <sub>2n</sub>

.	.	.		.
.	.	.		.
.	.	.		.
$M_m$	$T_{m1}$	$T_{m2}$	.....	$T_{mn}$

**IV. CONCLUSION**

In this paper, we have introduced a new method Advanced modified time deviation method. And also we prove this method for some numerical examples with n-jobs 2-machine, n-jobs 3machine and also for n-jobs m-machine. In future this method can be extended to process for sequencing the machine problems, such as n-job 2-machine or more than 2-machine with or without using this method.

**V. REFERENCES**

[1]. Joss Sanchez-Perez, "A Payoff System for Job Scheduling Problems", Journal of Applied Mathematics Sciences, Vol. 5, No. 19, pp.911 – 920, 2011.

[2]. Surekha P, S.Sumathi, "Solving Fuzzy based Job Shop Scheduling Problems using Ga and Aco", Journal of Emerging Trends in Computing and Information Sciences, Vol. 1, No. 2, Oct 2010.

[3]. Pervaiz Iqbal, Dr. P. S. Sheik Uduman and Dr. S. Srinivasan," Job Sequencing Problem Using Advanced Heuristics Techniques, Proceeding of the International Conference on Applied Mathematics and Theoretical Computer Science, 978-93-82338-35-2.(ISBN) 2013.

[4]. N. Nagamalleswara Rao<sup>1</sup>Dr. O. Naga Raju<sup>2</sup> and Prof. I. Ramesh Babu<sup>3</sup>, "Modified Heuristics Time Deviation Techniques for Job Sequencing and Computing of Minimum Total Elapsed Time, International Journal of Computer Science & Informing Technology (IJCSIT), Vol.5, No. 3, June 2013.