# High -Frequency AC Power Distribution For 25-Level Multilevel Inverter Using Switched - Capacitor 

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#### Abstract

High frequency transmission distribution has more advantages than low or, medium frequency in various kind of power system applications. In High frequency ac (HFAC) power distribution system, High frequency inverter serves as a source side. But, it is complex to obtain a high-frequency inverter with both simple circuit topologies and straight forward modulation strategy. So , in this paper we are proposed a novel switched -capacitor-based cascaded, which is constructed by a multilevel inverter, which is constructed by a H-Bridge backend and switched-capacitor frontend. By the conversion of series and parallel connections, the switched capacitor frontend increases the number of voltage levels. The output harmonics and the component counter can be significantly reduced by the increasing number of voltage levels. A symmetrical triangular waveform modulation is proposed with a simple analog implementation and low modulation frequency comparing with traditional multicarrier modulation. The circuit topology, symmetrical modulation, operation cycles, Fourier analysis, parameter determination, and topology enhancement are examined. An experimental prototype with a rated output frequency of 25 kHz is implemented to compare with simulation results. The experimental results agreed very well with the simulation that confirms the feasibility of proposed multilevel inverter.


Keywords : Cascaded H-Bridge, high-frequency ac (HFAC), multilevel inverter, switched capacitor (SC), symmetrical phase shift modulation (PSM), Total Harmonic Distortion (THD), Harmonics.

## I. INTRODUCTION

HIGH-FREQUENCY ac (HFAC) power
distribution system (PDS) becomes an
alternative to traditional dc distribution due to the less components and lower cost. The existing applications can be found in computer [1], telecom [2], electric vehicle [3], and renewable
energy microgrid [4], [5]. However, HFAC PDS has to overcome the challenges from large power capacity, high electromagnetic interference (EMI), and severe power losses [6].
A traditional HFAC PDS is made up of a highfrequency (HF) inverter, an HF transmission track, and numerous voltage-regulation modules (VRM). HF inverter accomplishes the power conversion to accommodate the requirement of point of load (POL). In order to increase the power capacity, the most popular method is to connect the inverter output in series or in parallel. However, it is impractical for HF inverter, because it is complicated to simultaneously synchronize both amplitude and phase with HF dynamics. Multilevel inverter is an effective solution to increase power capacity without synchronization consideration, so the higher power capacity is easy to be achieved by multilevel inverter with lower switch stress. Nonpolluted sinusoidal waveform with the lower total harmonic distortion (THD) is critically caused by long track distribution in HFAC PDS. The higher number of voltage levels can effectively decrease total harmonics content of staircase output, thus significantly simplifying the filter design [7]. HF power distribution is applicable for small scale and internal closed electrical network in electric vehicle (EV) due to moderate size of distribution network and effective weight reduction [8]. The consideration of operation frequency has to make compromise between the ac inductance and resistance [9], so multilevel inverter with the output frequency of about 20 kHz is a feasible trial to serve as power source for HF EV application.
The traditional topologies of multilevel inverter mainly are diode-clamped and capacitorclamped type [10], [11]. The former uses diodes to clamp the voltage level, and the latter uses additional capacitors to clamp the voltage. Voltage levels can then be obtained in a higher manner; however, the circuit becomes extremely complex in these two topologies. Another kind
of multilevel inverter is cascaded H -Bridge constructed by the series connection of H Bridges [12], [13]. The basic circuit is similar to the classical H-bridge DC-DC converter [14]. The cascaded structure increases the system reliability because of the same circuit cell, control structure and modulation. However, the disadvantages confronted by cascaded structure are more switches and a number of inputs. In order to increase two voltage levels in staircase output, an H -Bridge constructed by four power switches and an individual input are needed. Theoretically, cascaded H-Bridge can obtain staircase output with any number of voltage levels, but it is inappropriate to the applications of cost saving and input limitation. A number of studies have been performed to increase the number of voltage levels. A switched-capacitor (SC) based multilevel circuit can effectively increase the number of voltage levels. However, the control strategy is complex, and EMI issue becomes worse due to the discontinuous input current [15]. A single-phase five-level pulse width-modulated (PWM) inverter is constituted by a full bridge of diodes, two capacitors and a switch. However, it only provides output with five voltage levels, and higher number of voltage levels is limited by circuit structure [16]. An SCbased cascaded inverter was presented with SC frontend and full bridge backend. However, both complicated control and increased components limit its application [17]. The further study was presented using series/parallel conversion of SC. However, it is inappropriate to the applications with HF output because of multicarrier PWM (MPWM) [18], [19]. If output frequency is around 20 kHz , the carrier frequency reaches a couple of megahertz. Namely, the carrier frequency in MPWM is dozens times of the output frequency. Since the carrier frequency determines the switching frequency, a high switching loss is inevitable for the sake of highfrequency output. A boost multilevel inverter based in partial charging of SC can increase the
number of voltage levels theoretically. However, the control strategy is complicated to implement partial charging [20]. Therefore, it is a challenging task to present an SC-based multilevel inverter with high-frequency output, low-output harmonics, and high conversion efficiency [21]. Based on the study situation aforementioned, a novel multilevel inverter and simple modulation strategy are presented to serve as HF power source. The rest of this paper is organized as follows. The discussions of ninelevel inverter are presented in Section II, including circuit topology, modulation strategy, operation cycle, and Fourier analysis. The parameter determination and loss analysis are discussed in Section III. The further enhancement of 25 -level inverter is studied in Section IV.

## II. SC-BASEDCASCADED 9-LEVEL MULTI LEVEL INVERTER

The proposed circuit is made up of the SC frontend and cascaded H -Bridge backend. If the numbers of voltage levels obtained by SC frontend and cascaded H-Bridge backend are N1 and N 2 , respectively, the number of voltage levels is $2 \times \mathrm{N} 1 \times \mathrm{N} 2+1$ in the entire operation cycle.
A. Circuit Topology

Fig. 1 shows the circuit topology of nine-level inverter ( $\mathrm{N} 1=2, \mathrm{~N} 2=2$ ), where $S_{1}, S_{2}, S_{1}^{\prime}, S_{2}^{\prime}$ as the switching devices of SC circuits ( $S C_{1}$ and $S C_{2}$ ) are used to convert the series or parallel connection of $C_{1}$ and $C_{2} . S_{1 a}, S_{1 b}, S_{1 c}, S_{1 d}, S_{2 a}$, $S_{2 b}, S_{2 c}, S_{2 d}$ are the switching devices of cascaded H-Bridge. $V_{d c 1}$ and $V_{d c 2}$ are input voltage. $D_{1}$ and $D_{2}$ are diodes to restrict the current direction. $i_{\text {out }}$ and $V_{o}$ are the output current and the output voltage, respectively. It is worth noting that the backend circuit of the proposed inverter is cascaded H -Bridges in series connection. It is significant for H-Bridge to
ensure the circuit conducting regardless of the directions of output voltage and current. In other words, H-Bridge has four conducting modes in the conditions of inductive and resistive load, i.e., forward conducting, reverse conducting, forward freewheeling, and reverse freewheeling.
B. Modulation techniques

There are many modulation methods to regulate the multilevel inverter, the popular modulations are the space vector modulation [22], the multicarrier PWM [23], and the selective harmonic elimination [24], [25], subharmonic pulse width modulation [26], etc. However, most of them greatly increase the carrier frequency that is dozen times the frequency of reference or output. A symmetrical phase-shift modulation (PSM) is introduced into the proposed multilevel inverter.


Fig. 1. Circuit topology of cascaded nine-level inverter $(\mathrm{N} 1=2, \mathrm{~N} 2=2)$.

(a)

(b)

Fig. 2. Circuit of symmetrical PSM. (a) Circuit of symmetrical PSM. (b) Operational waveforms of symmetrical PSM.
The symmetrical PSM ensures the output voltage of full bridge is symmetrical to the carrier, so voltage levels can be superimposed symmetrically and carrier frequency is twice as that of the
output frequency [27]. The structure of f symmetrical PSM is shown in Fig. 2(a), and the operational waveform of symmetrical PSM is shown in Fig. 2(b).
The logic operations of gate signals used here are
gate $1=\operatorname{XOR}\{\mathrm{Q}(\mathrm{RS}), \bar{Q}(\mathrm{D})\}$
gate2 $=\operatorname{XOR}\{\mathrm{Q}(\mathrm{RS}), \mathrm{Q}(\mathrm{D})\}$
gate3 $=\operatorname{XOR}\{\operatorname{AND}\{\mathrm{Q}(\mathrm{RS}), \operatorname{NOT}(\mathrm{PW} M)\}, \mathrm{Q}(\mathrm{D})\}$ gate $4=\operatorname{XOR}\{\operatorname{AND}\{\mathrm{Q}(\mathrm{RS}), \operatorname{NOT}(\mathrm{PW} M)\}, \bar{Q}(\mathrm{D})\}$.

A controlled PWM with pulse width $\delta$ is symmetrically generated by the comparisons of the triangle carrier $V_{c}$ and modulation signal $V_{m}$. The rising edge matching of $V_{c}$ and $V_{m}$ triggers the polarity inversion of the leading bridge, while the falling edge matching of $V_{c}$ and $V_{m}$ triggers the polarity inversion of the lagging bridge. When $V_{m}$ has a change $\Delta V_{m}$, this modulation simultaneously moves gate1 and gate3 in the opposite direction. Thus, the derived $V_{a b}$ is symmetrical with respect to $V_{c}$.
C. Operational cycles

Fig. 3 demonstrates the ideal waveforms of proposed inverter. $V_{c}$ is the triangular carrier, and $V_{p p}$ is the peak value of $V_{c}$. The modulation signals of triangular carrier are $V_{m_{-} 1 c}, V_{m_{-} 1 b}, V_{m_{-} 2 c}$ and $V_{m_{-} 2 b}, V_{m_{-} 1 b}$ and $V_{m_{-} 2 b}$ are used to control phase-shift angles of H -Bridge 1 and H -Bridge 2 , respectively, and $\delta i$ is the duration of voltage levels controlled by them. $V_{m_{-} 1 c}$ and $V_{m_{-} 2 c}$ are used to control the alternative operations of $S C_{1}$ and $S C_{2}$, respectively, and $\alpha$ is the duration of voltage levels controlled by them. Thus, the drive signals of H -Bridge switches ( $S_{1 a}, S_{1 b}, S_{1 c}$, $S_{1 d}, S_{2 a}, S_{2 b}, S_{2 c}, S_{2 d}$ ) are phase-shifted pulse signals, while the drive signals of SC switches ( $S_{1}$, $S_{2}, S_{1}^{\prime}, S_{2}^{\prime}$ ) are complementary pulse signals. Two operational modes are presented as shown in Fig. 3 (a) and (b). Mode 1 is similar to mode 2 apart from the different positions of modulation signals $\left(V_{m_{-} 1 c}, V_{m_{-} 1 b}, V_{m_{-} 2 c}, V_{m_{-} 2 b}\right)$. Consequently, the durations of each voltage level are controlled by modulation signals in both mode 1 and mode 2.

Active circuits of the operational mode 1 are demonstrated in Fig. 4. Re is the equivalent load. When t satisfies $t_{0} \leq \mathrm{t}<t_{1}$ in Fig. 3(a), the switches $S_{1 a}, S_{1 b}, S_{2 a}, S_{2 b}$ are driven by the gate-source voltage, respectively. H -Bridges 1 and 2 are in freewheeling state, and output voltage equals 0 . Because $S_{1}^{\prime}$ and $S_{2}^{\prime}$ are on, the capacitors $C_{1}$ and $C_{2}$ are charged to $V_{i n}\left(V_{d c 1}=V_{d c 2}=V_{i n}\right)$. The voltages on Bus 1 and Bus 2 are Vin as well. The current flow of this time interval is shown in Fig. 4(a).
When t satisfies $t_{1} \leq \mathrm{t}<t_{2}$ in Fig. 3(a), the switches $S_{1 a}, S_{1 b}, S_{2 a}, S_{2 c}$ are driven by the gate-source voltage, respectively. H -Bridge 1 is in freewheeling state, and H-Bridge 2 is in positive conducting state. Output voltage equals $V_{\text {in }}$. Because $S_{1}^{\prime}$, and $S_{2}^{\prime}$ are on, the capacitors $C_{1}$ and $C_{2}$ keep charged to $V_{i n}\left(V_{d c 1}=V_{d c 2}=V_{i n}\right)$. The voltages on Bus 1 and Bus 2 are $V_{i n}$ as well. The current flow of this time interval is shown in Fig. 4(b).
When t satisfies $t_{2} \leq \mathrm{t}<t_{3}$ in Fig. 3(a), the switches $S_{1 a}, S_{1 c}, S_{2 a}, S_{2 c}$ are driven by the gate-source voltage, respectively. H -Bridges 1 and 2 are in positive conducting state. Output voltage equals $2 V_{\text {in }}$. Because $S_{1}^{\prime}$, and $S_{2}^{\prime}$ are on, the capacitors $C_{1}$ and $C_{2}$ keep charged to $V_{i n}\left(V_{d c 1}=\right.$ $\left.V_{d c 2}=V_{i n}\right)$. The voltages on Bus 1 and Bus 2 are Vin as well. The current flow of this time interval is shown in Fig. 4(c).

(a)

When t satisfies $t_{3} \leq \mathrm{t}<t_{4}$ in Fig. 3(a), the switches $S_{1 a}, S_{1 c}, S_{2 a}, S_{2 c}$ are driven by the gate-source voltage, respectively. H-Bridges 1 and 2 are in positive conducting state. Output voltage equals $3 V_{\text {in }}$. Because $S_{1}^{\prime}$, and $S_{2}^{\prime}$ are on, the capacitor $C_{1}$ keeps charged to $V_{i n}\left(V_{d c 1}=V_{d c 2}=\right.$ $V_{\text {in }}$ ), and the capacitor C 2 is discharged. The voltages on Bus 1 and Bus 2 are $V_{\text {in }}$ and $2 V_{\text {in }}$, respectively. The current flow of this time interval is shown in Fig. 4(d)..


Fig. 3. Operational waveforms of the proposed multilevel inverter. (a) Operational mode 1. (b) Operational mode 2.


When t satisfies $t_{4} \leq \mathrm{t}<t_{5}$ in Fig. 3(a), the switches $S_{1 a}, S_{1 c}, S_{2 a}, S_{2 c}$ are driven by the
gate-source voltage, respectively. H -Bridges 1 and 2 are in positive conducting state. Output voltage equals $4 V_{\text {in }}$. Because $S_{1}$ and $S_{2}$ are on, the capacitor $C_{1}$ and $C_{2}$ are discharged. The voltages on Bus 1 and Bus 2 both are $2 V_{\text {in }}$. The current flow of this time interval is shown in Fig. 4(e).


Fig. 4. Active circuits for different operation intervals in the operational mode 1: (a) $t_{0}-t_{1}$; (b) $t_{1}-t_{2}$; (c) $t_{2}-t_{3}$; (d) $t_{3}-t_{4}$; (e) $t_{4}-t_{5}$; (f) $t_{5}-t_{6}$; (g) $t_{6}-t_{7}$; (h) $t_{7}-t_{8}$

The operations in $t_{5} \leq \mathrm{t}<t_{6}, t_{6} \leq \mathrm{t}<t_{7}$, and $t_{7} \leq \mathrm{t}$ $<t_{8}$, are the same as the operations in $t_{3} \leq \mathrm{t}<t_{4}$, $t_{2} \leq \mathrm{t}<t_{3}$, and $t_{1} \leq \mathrm{t}<t_{2}$, respectively. The active circuits are shown in Fig. 4(f)-(h). Comparing with operational mode 1 , the mode 2 has the different active circuits in twotime intervals. When t satisfies $t_{2} \leq \mathrm{t}<t_{3}$ in operational mode 2 as shown in Fig. 3(b), the switches $S_{1 a}, S_{1 b}, S_{2 a}, S_{2 c}$ are driven by the gate-source voltage, respectively. H -Bridge 1 is in freewheeling state, and H -Bridge 2 is in


Fig. 5. Active circuits for different operation intervals in the operational mode 2: (a) $t_{2}-t_{3}$; (b) $t_{6}-t_{7}$.
positive conducting state. Output voltage equals $2 V_{\text {in }}$. Because $S_{1}$ and $S_{2}$ are on, the capacitor $C_{1}$ keeps charged to $V_{i n}$ and capacitor $C_{2}$ is discharged. The voltages on Bus 1 and Bus 2 are Vin and $2 V_{\text {in }}$, respectively. The current flow of this time interval is shown in Fig. 5(a). Similarly, the active circuit of $t_{6} \leq \mathrm{t}<t_{7}$ is shown in Fig. 5(b) that has the same operations as $t_{2} \leq \mathrm{t}<t_{3}$.
The second half-cycle (from $t_{8}$ on) has the similar active circuits as the first half-cycle ( $t_{1}-t_{8}$ ), but the current will be circulated in the opposite direction to provide the negative output voltage. The relations of on-state switches and output voltage level are described in Table I, as well as operations of two modes are compared closely. Table I has ten working states for nine voltage levels. When the operation enters a new state from an adjacent state, only one power switch changes between on and off. The device stress in switching devices of H -bridge circuit is higher than that in SC circuit. It can also be found that the output voltage in Mode 1 is more stable than Mode 2 due to less discharging period of switching capacitor.

TABLEI
Relations of On-State Switches and Output Voltage

| Mode1 |  |  |  | Mode2 |  |  |
| :--- | :---: | :--- | :--- | :--- | :--- | :---: |
| On-state <br> switches | Out <br> put <br> volt <br> age | Capacit <br> or state | On-state <br> switches | Out <br> put <br> volt <br> age | Capacito <br> r state |  |
| $\mathrm{S}_{1 \mathrm{a}}, \mathrm{S}_{1 \mathrm{c}}, \mathrm{S}_{2 \mathrm{a}}$, <br> $\mathrm{S}_{2 \mathrm{c}}, \mathrm{S}_{1}, \mathrm{~S}_{2}$ | $4 \mathrm{~V}_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Dischar <br> ging | $\mathrm{S}_{1 \mathrm{a}}, \mathrm{S}_{1 \mathrm{c}}, \mathrm{S}_{2 \mathrm{a}}$, <br> $\mathrm{S}_{2 \mathrm{c}}, \mathrm{S}_{1}, \mathrm{~S}_{2}$ | $4 \mathrm{~V}_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Discharg <br> ing |  |
| $\mathrm{S}_{1 \mathrm{a}}, \mathrm{S}_{1 \mathrm{c}}, \mathrm{S}_{2 \mathrm{a}}$, <br> $\mathrm{S}_{2 \mathrm{c}}, \mathrm{S}_{1}^{\prime}, \mathrm{S}_{2}$ | $3 \mathrm{~V}_{\text {in }}$ | $\mathrm{C}_{2}$ <br> Dischar <br> ging | $\mathrm{S}_{1 \mathrm{a}}, \mathrm{S}_{1 \mathrm{c}}, \mathrm{S}_{2 \mathrm{a}}$, <br> $\mathrm{S}_{2 \mathrm{c}}, \mathrm{S}_{1}^{\prime}, \mathrm{S}_{2}$ | $3 \mathrm{~V}_{\text {in }}$ | $\mathrm{C}_{2}$ <br> Discharg <br> ing |  |


| $\begin{aligned} & \mathrm{S}_{1 \mathrm{a}}, \mathrm{~S}_{1 \mathrm{c}}, \mathrm{~S}_{2 \mathrm{a}} \\ & \mathrm{~S}_{2 \mathrm{c}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2}^{\prime} \end{aligned}$ | $2 V_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Chargi ng | $\begin{aligned} & \mathrm{S}_{1 \mathrm{a}}, \mathrm{~S}_{1 \mathrm{~b}}, \mathrm{~S}_{2 \mathrm{a}} \\ & \mathrm{~S}_{2 \mathrm{c}}, S_{1}^{\prime}, S_{2} \end{aligned}$ | $2 V_{\text {in }}$ | $\mathrm{C}_{2}$ Discharg ing |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \mathrm{S}_{1 \mathrm{a}}, \mathrm{~S}_{1 \mathrm{~b}}, \mathrm{~S}_{2 \mathrm{a}}, \\ & \mathrm{~S}_{2 \mathrm{c}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2}^{\prime} \end{aligned}$ | $\mathrm{V}_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Chargi ng | $\begin{aligned} & \mathrm{S}_{1 \mathrm{a}}, \mathrm{~S}_{1 \mathrm{~b}}, \mathrm{~S}_{2 \mathrm{a}}, \\ & \mathrm{~S}_{2 \mathrm{c}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2}^{\prime} \end{aligned}$ | $V_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Charging |
| $\begin{aligned} & \mathrm{S}_{1 \mathrm{a}}, \mathrm{~S}_{1 \mathrm{~b}}, \mathrm{~S}_{\mathrm{ad}}, \\ & \mathrm{~S}_{2 \mathrm{~b}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2}^{\prime} \text { or } \\ & \mathrm{S}_{1 \mathrm{c}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{c}}, \\ & \mathrm{~S}_{2 \mathrm{~d}} \\ & \hline \end{aligned}$ | 0 | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Chargi ng | $\begin{aligned} & \mathrm{S}_{1 \mathrm{a}}, \mathrm{~S}_{1 \mathrm{~b}}, \mathrm{~S}_{\mathrm{az}} \\ & \mathrm{~S}_{2 \mathrm{~b}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2}^{\prime} \text { or } \\ & \mathrm{S}_{1 \mathrm{c}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{c}}, \\ & \mathrm{~S}_{2 \mathrm{~d}} \\ & \hline \end{aligned}$ | 0 | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Charging |
| $\begin{aligned} & \mathrm{S}_{1 \mathrm{c}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{~b}}, \\ & \mathrm{~S}_{2 \mathrm{~d}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2}^{\prime} \end{aligned}$ | $-V_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Chargi <br> ng | $\begin{aligned} & \mathrm{S}_{1 \mathrm{c}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{~b}} \\ & \mathrm{~S}_{2 \mathrm{~d}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2}^{\prime} \end{aligned}$ | $-V_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Charging |
| $\begin{aligned} & \mathrm{S}_{1 \mathrm{~b}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{~b}}, \\ & \mathrm{~S}_{2 \mathrm{~d}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2}^{\prime} \end{aligned}$ | $2 V_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Chargi <br> ng | $\begin{aligned} & \mathrm{S}_{1 \mathrm{c}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{~b}}, \\ & \mathrm{~S}_{2 \mathrm{~d}}, \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2} \end{aligned}$ | $2 V_{\text {in }}$ | $\mathrm{C}_{2}$ Discharg ing |
| $\begin{aligned} & \mathrm{S}_{1 \mathrm{~b}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{~b}}, \mathrm{~S}_{2 \mathrm{~d}} \\ & , \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2} \end{aligned}$ | $3 V_{\text {in }}$ | $\mathrm{C}_{2}$ <br> Dischar ging | $\begin{aligned} & \mathrm{S}_{1 \mathrm{~b}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{~b}}, \mathrm{~S}_{2 \mathrm{~d}} \\ & , \mathrm{~S}_{1}^{\prime}, \mathrm{S}_{2} \end{aligned}$ | $3 V_{\mathrm{in}}$ | $\mathrm{C}_{2}$ <br> Discharg <br> ing |
| $\begin{aligned} & \mathrm{S}_{1 \mathrm{~b}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{~b}}, \\ & \mathrm{~S}_{2 \mathrm{~d}}, \mathrm{~S}_{1}, \mathrm{~S}_{2} \end{aligned}$ | $4 V_{\text {in }}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ <br> Dischar <br> ging | $\begin{aligned} & \mathrm{S}_{1 \mathrm{~b}}, \mathrm{~S}_{1 \mathrm{~d}}, \mathrm{~S}_{2 \mathrm{~b}} \\ & \mathrm{~S}_{2 \mathrm{~d}}, \mathrm{~S}_{1}, \mathrm{~S}_{2} \end{aligned}$ | $4 V_{\mathrm{in}}$ | $\begin{aligned} & \hline \mathrm{C}_{1}, \mathrm{C}_{2} \\ & \text { Discharg } \\ & \text { ing } \\ & \hline \end{aligned}$ |

Along with the up-down movement of modulation signals ( $V_{m_{-} 1 c}, V_{m_{-} 1 b}, V_{m_{-} 2 c}, V_{m_{-} 2 b}$ ), the output voltage of the proposed inverter is a controllable nine-level staircase. The duration of each voltage level is determined by the dutycycle of SC circuit and the phase-shifted angle of H -Bridge circuit.
D. Operation Cycles

In aforementioned nine-level inverter, the staircase output vo can be divided into four components $V_{o 1}, V_{o 2}, V_{o 3}$, and $V_{o 4}$, as shown in Fig. 6. The durations of each component are decided by the comparisons of reference signal $\left(V_{m_{-} 1 c}, V_{m_{-} 1 b}, V_{m_{-} 2 c}, V_{m_{-} 2 b}\right)$ and triangular carrier ( $V_{c}$ ). If pulse widths of the constituted component are defined as $\delta_{1}, \delta_{2}, \alpha_{1}$, and $\alpha_{2}$, Fourier analysis is accomplished for this ninelevel staircase. The magnitude of the harmonics is derived by

$$
\begin{align*}
V_{n}= & \frac{4 V_{i n}}{n \pi}\left(\cos \left(n\left(\frac{\pi-\alpha_{1}}{2}\right)\right)+\cos \left(n\left(\frac{\pi-\delta_{1}}{2}\right)\right)\right. \\
& \left.+\cos \left(n\left(\frac{\pi-\alpha_{2}}{2}\right)\right)+\cos \left(n\left(\frac{\pi-\delta_{2}}{2}\right)\right)\right)  \tag{3}\\
& \mathrm{n}=1,3,5 \ldots .
\end{align*}
$$



Fig. 6. Output voltage decomposition for Fourier analysis in mode1
In operation mode 1

$$
\begin{array}{ll}
\delta_{1}=\frac{V_{m_{-} 2 b}}{V_{p p}} \pi, & \alpha_{1}=\frac{V_{m_{-}-1 b}}{V_{p p}} \pi, \\
\delta_{2}=\frac{V_{m_{-2} c}}{V_{p p}} \pi, & =\frac{V_{m_{-} 1 c}}{V_{p p}} \pi .
\end{array}
$$

In operation mode 2

$$
\begin{array}{ll}
\delta_{1}=\frac{V_{m_{2}-2}}{V_{p p}} \pi, & \alpha_{1}=\frac{V_{m_{2} 2 c}}{V_{p p}} \pi, \\
\delta_{2}=\frac{V_{m_{-} b}}{V_{p p}} \pi, & =\frac{V_{m_{-} 1 c}}{V_{p p}} \pi .
\end{array}
$$

To further describe the relations of output THD and pulsewidths $\alpha_{1}, \alpha_{2}, \delta_{1}, \delta_{2}$, four parameters are predefined

$$
\begin{array}{lll}
k_{1}=\frac{\alpha_{1}}{\delta_{1}}, \quad k_{2}=\frac{\alpha_{2}}{\delta_{2}}, & \begin{array}{l}
x_{1} \\
=\frac{\pi-\delta_{1}}{2},
\end{array} & \begin{array}{l}
x_{2} \\
=\frac{\pi-\delta_{2}}{2}
\end{array} \tag{6}
\end{array}
$$

The output waveforms can be characterized by these four constants. According to the definitions as (THD $=\left(\sqrt{\sum_{n=2 \ldots . . . .}^{\infty} V_{n}^{2} / V_{1}}\right) \times 100 \%$ ) THD of output voltage can be calculated by the harmonic magnitudes. The relations of outp ut THD to $x_{1}, x_{2}$ are given in Fig. 7 with the fixed $k_{1}$ and $k_{2}$.


Fig. 7. Relation curves of output THD versus $x_{1}$, $x_{2}$ (unit, rad): (a) $k_{1}=0.6, k_{2}=0.4$; (b) $k_{1}=0.5$, $k_{2}=0.5$.
It can be found from Fig. 7 that THD is easy to be regulated by the duration width of voltage levels. At the suitable scope of $x_{1}$ and $x_{2}$, THD of output voltage is less than $10 \%$. When $k_{1}=0.6$, $k_{2}=0.4$, THD can be less than $10 \%$ within the scope of $0.05<x_{1}<0.5$ and $0.4<x_{2}<0.6$. When $k_{1}=0.5, k_{2}=0.5$, THD can be less than $10 \%$ within the scope of $0<x_{1}<0.4$ and $0.4<x_{2}<0.6$. Furthermore, THD becomes less along with the increasing number of voltage levels. The output magnitude of multilevel inverter can be regulated by the duration width of voltage levels as well. Two patterns are available to perform the regulations of THD and magnitude simultaneously. One is to regulate $x_{1}, x_{2}$ with the fixed $k_{1}, k_{2}$. The other one is to regulate $k_{1}$, $k_{2}$ with the fixed $x_{1}, x_{2}$. The numerical benchmark and THD optimization will be examined in the future study, and a fixed ratio ( $k_{1}=k_{2}=0.5, x_{1}=\pi / 8, x_{2}=\pi / 4$ ) is adopted to evaluate output harmonics in subsequent simulation and experiment. If the proposed dc-ac inverter is used as second stage of ac-ac conversion, an ac-dc controlled rectifier is introduced as preceding stage of ac-ac conversion. Power factor correction (PFC) implemented by dc-dc converter can improve the power factor in ac -dc conversion. In this case, both SC and Hbridge generate the optimized pulse width to minimize output THD. The magnitude regulation of output voltage can be performed by controllable ac-dc stage in input side. The minimized THD is achieved by this two-stage power circuit, namely, ac-dc stage is used to
regulate magnitude, and dc-ac stage formed by the proposed inverter is used to minimize THD.

## III. CAPACITANCE CALCULATION

As shown in Fig. 4, the capacitors are in parallel with power source so they are charged, and the capacitors are discharged when they are in series with power source. The switch Si and $\mathrm{Sil}^{\mathrm{l}}$ are driven alternatively during the half of output cycle. Therefore, the driven frequency of $S_{i}$ and $S_{i}$ is twice the frequency of output voltage, as well as the driven frequency of $S_{i a}-S_{i d}$ is the same as the frequency of output voltage. The capacitance of $C_{i}$ is determined by the voltage ripple of $C_{i}$ that denotes the voltage fluctuation of multilevel output. The larger capacitance has the fewer ripple voltage. The voltage fluctuation over a narrow scope has a smaller power losses and higher capacitor efficiency. The appropriated method of capacitance calculation is that the maximum voltage ripple is $10 \%$ of the maximum capacitor voltage [28]. Before obtaining the capacitance of $C_{i}$, two assumptions are given to simplify the derivations: 1) the output load is pure resistive load, and 2) the same duration is given in each level of staircase output. Therefore, the time points in Fig. 3 are
$t_{0}=0, t_{1}=\frac{1}{20} t_{s}, t_{2}=\frac{1}{10} t_{s}, t_{3}=\frac{3}{20} t_{s}, t_{4}=\frac{1}{5} t_{s}$,
$t_{5}=\frac{3}{10} t_{s}, \quad t_{6}=\frac{7}{20} t_{s}, t_{7}=\frac{2}{5} \mathrm{ts}, t_{8}=\frac{9}{20} t_{s}$,
where ts is the period of the output voltage derived by

$$
\begin{equation*}
t_{s}=\frac{1}{f_{\mathrm{s}}} \tag{8}
\end{equation*}
$$

where fs is the frequency of the output voltage. In the operational mode 1, as shown in Fig. 3(a), the longest discharging cycle of $C_{1}$ is between $t_{4}$ and $t_{5}$, and the longest discharging cycle of $C_{2}$ is between $t_{3}$ and $t_{6}$. In the operational mode 2 , as shown in Fig. 3(b), the longest discharging cycle
of $C_{1}$ is the same as the operational mode 1 , while the longest discharging cycle of $C_{2}$ is between $t_{2}$ and $t_{7}$. Therefore, the maximum discharging amount of $C_{1}$ is $Q_{c 1}$ and is defined as

$$
\begin{equation*}
Q_{c 1}=\int_{t_{4}}^{t_{5}} I_{o u t} \sin \left(2 \pi f_{s} t-\phi\right) d t \tag{9}
\end{equation*}
$$

where $I_{\text {out }}$ is the amplitude of the output current $i_{\text {out }}$ and $\Phi$ is the phase difference between the output voltage $V_{o}$ and current iout. If $10 \%$ ripple voltage is considered, $Q_{c 1}$ should be less than $10 \%$ of the maximum charge of $C_{1}$, i.e.

$$
\begin{equation*}
C_{1} \geq \frac{Q_{c 1}}{0.1 V_{i n}} \tag{10}
\end{equation*}
$$

Furthermore, the maximum discharging amount of $C_{2}$ is $Q_{c 2}$ and is defined as
$Q_{c 2}=\int_{t_{3}}^{t_{6}} I_{\text {out }} \sin \left(2 \pi f_{s} t-\phi\right) d t$, mode 1
$Q_{c 2}=\int_{t_{2}}^{t_{7}} I_{\text {out }} \sin \left(2 \pi f_{s} t-\phi\right) d t$, mode 2
Then

$$
\begin{equation*}
C_{2} \geq \frac{Q_{c 2}}{0.1 V_{i n}} \tag{12}
\end{equation*}
$$

It can be seen from the equations that the operational mode 2 needs larger $C_{2}$ than that in operational mode 1 . When the load is resistive, the phase of load current is agreed with the load voltage. The maximum discharging amount of capacitor is obtained in resistive load, because the peak load current is the midpoint of integration period. In other words, if the capacitance of $C_{i}$ is derived in pure resistive load, it also maintains the less voltage ripples in inductive load.
The peak current of the capacitor $C_{i}$ is derived by

$$
\begin{equation*}
I_{c i}=\frac{V_{i n}-V_{C i}-V_{d F}}{r_{c}+r_{o n}+r_{d}} \tag{14}
\end{equation*}
$$

where $V_{C i}$ is the voltage on the capacitors $C_{i}, V_{d F}$ is the forward voltage drop of diode, $r_{c}$ is the equivalent series resistance (ESR) of the capacitors, ron is the internal on-state resistance of the switching device, and $r_{d}$ is the internal onstate resistance of the diode. Because of a small voltage difference of $V_{i n}$ and $V_{C i}$, the peak current $I_{c i}$ is fewer for the larger $C_{i}$. Thus, the larger capacitor is needed to cut down undesirable peak current and prolong the capacitor lifetime.
The analysis of switching loss is similar to the traditional cascaded H-bridge, while the
capacitor losses consisting of ripple loss $P_{\text {rip }}$ and conduction loss $P_{\text {cond }}$ are newly introduced by the proposed inverter. When the capacitor $C_{i}$ is connected from series to parallel, the ripple is derived by the difference between the input voltage $V_{i n}$ and the capacitor voltage $V_{c i}$. The voltage ripple of $C_{i}$ is

$$
\begin{equation*}
\Delta V_{\text {rip }}=\frac{1}{c_{i}} \int_{t_{-}}^{t_{+}} i_{C_{i}} d t \tag{15}
\end{equation*}
$$

where $i_{C_{i}}$ is the transient current of the capacitor $C_{i}$, and the discharging interval is denoted by $t_{-}$ and $t_{+}$. For C1 in operational mode $1, t_{-}$and $t_{+}$ are $t_{4}$ and $t_{5}$, respectively. For $C_{2}$ in operational mode $1, t_{-}$and $t_{+}$are $t_{3}$ and $t_{6}$, respectively. Thus, the loss from voltage ripple is resulted by

$$
\begin{equation*}
P_{r i p}=\sum_{i=1}^{k} C_{i} \Delta V_{r i p}^{2} f_{s} \tag{16}
\end{equation*}
$$

where k is the number of switched capacitors (SCs), and $f_{s}$ is the frequency of the output voltage. It can be found that the ripple loss is inversely proportional to the capacitor $C_{i}$. The conduction losses can be further calculated by

$$
\begin{equation*}
P_{\text {cond }}=2 f_{s} \sum_{i=1}^{k} \int_{t_{-}}^{t_{+}} r_{c} i_{c_{i}}^{2} d t \tag{17}
\end{equation*}
$$

The larger capacitor current leads to a large conduction loss. Lastly, the losses from SCs are denoted by

$$
\begin{equation*}
P_{s c}=P_{\text {rip }}+P_{\text {cond }} \tag{18}
\end{equation*}
$$

Both ripple loss and conduction loss are proportional to the frequency of the output voltage and number of capacitors. It is concluded that a larger capacitor can improve efficiency and prolong capacitor lifetime. However, the larger capacitor leads to the higher cost. Thus, a tradeoff of cost and efficiency need to be taken into account.
According to (10), (13), and (15), the relation curves of SCs ( $C_{i}$ ) and ripple voltage are illustrated in Fig. 8(a) with the fixed 25 kHz output frequency, and relation curves of SC $\left(C_{i}\right)$ and output frequency are illustrated in Fig. 8(b) with the fixed $10 \%$ ripple voltage.


Fig. 8. Capacitance determination. (a) Curves of frontend capacitor versus voltage ripple with 25 kHz output frequency. (b) Curves of frontend capacitor versus output frequency with $10 \%$ voltage ripple.
It can be found from Fig. 8(a) that the less capacitance leads to larger ripple voltage. Operational mode 2 needs larger capacitance than mode 1 to keep the ripples low. The gradient of capacitor to ripple is larger in low-ripple zone, and the gradient of capacitor to ripple is lower in high-ripple zone. The gradient variation is caused by inversely proportional relation between capacitance with ripple voltage. It can be found from Fig. 8(b) that the less capacitance is required for higher frequency applications to maintain $10 \%$ ripple voltage. Thus, capacitor cost can be greatly saved for HF application compared with low frequency counterpart.

## IV. FURTHER ENHANCEMENTS

The number of voltage levels can be further increased via two approaches. One is to increase the level number generated by SC circuit; the other one is to increase level number generated by cascaded H -Bridge.


Thirteen-level inverters, as shown in Fig. 9, explain these two methods. A $3 \times 2$ structure, as shown in Fig. 9(a), is derived by the enhancement of SC circuit, which needs 6 diodes, 4 capacitors, 14 switches, and 2 dc inputs. $2 \times 3$ structure as shown in Fig. 9(b) is derived by the enhancement of H-Bridge circuit, which needs 3 diodes, 3 capacitors, 18 switches, and 3 dc inputs.


Fig. 9. Circuit topology of 25 -level inverter. (a) 3 $\times 2$ with two dc inputs. (b) $2 \times 3$ with three dc inputs.
It can be found that $3 \times 2$ structure requires more diodes and capacitors than $2 \times 3$ structure. However, the number of power switches in $3 \times 2$ structure is less than that in $2 \times 3$ structure.

TABLEII
ON STATE SWITCHSES OF 25-LEVEL

| ON STATE SWITCHES | OUTPUT VOLTAGE(v) | CAPACITOR STATE |
| :---: | :---: | :---: |
| $\mathrm{S}_{1}$ to $\mathrm{S}_{6}, \mathrm{~S}_{1 \mathrm{a}}$ to $\mathrm{S}_{69}$ | $12 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 discharging |
| $\mathrm{S}_{1}$ to $\mathrm{S}_{5}, \mathrm{~S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6}$ | $11 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to $\mathrm{C}_{5}$ discharging, $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1}$ to $\mathrm{S}_{4}, \mathrm{~S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6}$ | 10 Vm | $\mathrm{C}_{1}$ to $\mathrm{C}_{4}$ discharging, $\mathrm{C}, \mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1}$ to $\mathrm{S}_{3}, \mathrm{~S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6 \mathrm{a}}$ | $9 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to $\mathrm{C}_{3}$ discharging, $\mathrm{C}_{4}$ to $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1}, \mathrm{~S}_{2}, \mathrm{~S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6 \mathrm{a}}$ | 8 Vm | $\mathrm{C}_{1}, \mathrm{C}_{2}$ discharging, $\mathrm{C}_{3}$ to $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1}, \mathrm{~S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6}{ }^{\text {a }}$ | $7 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ discharging, $\mathrm{C}_{2}$ to $\mathrm{C}_{6}$ charging |
| S ${ }_{\text {a }}$ to S6a | 6 Vm | $\mathrm{C}_{1}$ to C6 charging |
| $\mathrm{S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6 \mathrm{a}} \mathrm{S}_{\text {S }}$ b | $5 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 charging |
| $\mathrm{S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6 \mathrm{a}, \mathrm{S}} \mathrm{S}_{5}, \mathrm{~S}_{6 \mathrm{~b}}$ | $4 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 charging |
| $\mathrm{S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6 \mathrm{a}}, \mathrm{S}_{4 \mathrm{~b}}$ to $\mathrm{S}_{6 \mathrm{~b}}$ | $3 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 charging |


| $\mathrm{S}_{1 \mathrm{a}}$ to $\mathrm{S}_{6 \mathrm{a}} \mathrm{S}_{3} \mathrm{~b}$ to $\mathrm{S}_{6}$ | $2 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 charging |
| :---: | :---: | :---: |
|  | $\mathrm{V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to $\mathrm{C}_{6}$ charging |
|  | 0 | $\mathrm{C}_{1}$ to $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{2 \mathrm{a}}$ to $\mathrm{S}_{6 \mathrm{a}} \mathrm{S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6 \mathrm{~b}}$ | - $\mathrm{V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 charging |
| $\mathrm{S}_{3 \mathrm{a}}$ to $\mathrm{S}_{6 \mathrm{a}} \mathrm{S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6 \mathrm{~b}}$ | $-2 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 charging |
|  | $-3 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 charging |
| $\mathrm{S}_{5 \mathrm{a}}, \mathrm{S}_{6 \mathrm{a}, \mathrm{S}} \mathrm{S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6}$ | $-4 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{6 \mathrm{a}}, \mathrm{S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6 \mathrm{~b}}$ | $-5 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6 \mathrm{~b}}$ | $-6 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C6 charging |
| $\mathrm{S}_{1,} \mathrm{~S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6} \mathrm{~b}$ | $-7 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ discharging, $\mathrm{C}_{2}$ to $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1}, \mathrm{~S}_{2}, \mathrm{~S}_{1} \mathrm{~b}$ to $\mathrm{S}_{6 \mathrm{~b}}$ | $-8 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}, \mathrm{C}_{2}$ discharging, $\mathrm{C}_{3}$ to $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1}$ to $\mathrm{S}_{3}, \mathrm{~S}_{1}$ b to $\mathrm{S}_{6} \mathrm{~b}$ | $-9 \mathrm{Vm}$ | $\mathrm{C}_{1}$ to $\mathrm{C}_{3}$ discharging, $\mathrm{C}_{4}$ to $\mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1}$ to $\mathrm{S}_{4}, \mathrm{~S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6} \mathrm{~b}$ | $-10 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to $\mathrm{C}_{4}$ discharging, $\mathrm{C}_{5}, \mathrm{C}_{6}$ charging |
| $\mathrm{S}_{1}$ to $\mathrm{S}_{5}, \mathrm{~S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6} \mathrm{~b}$ | $-11 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{C}_{1}$ to C5 discharging, C6 charging |
| $\mathrm{S}_{1}$ to $\mathrm{S}_{6}, \mathrm{~S}_{1 \mathrm{~b}}$ to $\mathrm{S}_{6}$ b | $-12 \mathrm{Vm}$ | $\mathrm{C}_{1}$ to C6discharging |

Because the traditional cascaded H -bridge needs 24 switches and 6 inputs to produce 13 voltage levels, the numbers of power switches and inputs are greatly decreased by proposed inverter.

TABLEIII
COMPONENTS COMPARISON OF PROPOSED INVERTER AND CASCADED H-BRIDGE

| Inverter type | Proposed inverter enhanced by $\begin{gathered} \text { SC } \\ \mathrm{n} \times 2 \text { topology } \end{gathered}$ | Proposed inverter enhanced by H Bridge $2 \times n$ topology | Cascaded <br> H-Bridge |
| :---: | :---: | :---: | :---: |
| Switching <br> device | $2 \mathrm{n}+8$ | 6 n | 8 n |
| Capacitor | 2n-2 | n | 0 |
| Diode | 4n-6 | n | 0 |
| DC bus | 2 | n | 2 n |
| Power losses | $\begin{gathered} (2 \mathrm{n}-2) \operatorname{loss}_{\text {cap }}+(4 \mathrm{n}-6) \operatorname{loss}_{\text {diode }} \\ +(2 \mathrm{n}+8) \operatorname{loss}_{\text {switch }} \end{gathered}$ | nloss $_{\text {cap }}+$ nloss $_{\text {diode }}$ +6 loss $_{\text {swith }}$ | $8 \mathrm{nloss}_{\text {switch }}$ |

In order to accomplish the staircase output with $4 n+1$ voltage levels, the component counts are compared in Table III.



Fig. 10. Simulation waveforms of nine-level SCbased cascaded inverter, output frequency $f_{s}=25$ $\mathrm{kHz}\left(k_{1}=k_{2}=0.5, x_{1}=\pi / 8, x_{2}=\pi / 4\right.$, mode 1 ). (a) Low power at 50 W . (b) High power at 4 kW .
An $n \times 2$ topology needs $2 n-2$ capacitors, $2 n+8$ switches, and 2 dc inputs; $2 \times \mathrm{n}$ topology needs n capacitors, 6 n switches, and n dc inputs. The traditional cascaded H -Bridge needs 8 n switches and 2 n dc inputs. With the same number of voltage levels, the proposed inverter needs less switching devices and inputs than the traditional cascaded H-Bridge. Considering the power losses, the traditional cascaded H -bridge has the higher switching losses caused by more switch devices. However, the proposed inverter newly introduces the capacitor loss that has already been examined in last section. Moreover, a flexible circuit structure becomes possible. It is feasible for the proposed multilevel inverter to select suitable enhancement that can accommodate the requirements from different applications. For example, $2 \times n$ topology can be used for the power application sourced by multiple solar panels or batteries, and $\mathrm{n} \times 2$ topology can be used for the power application sourced by dual power sources.

## V. PERFORMANCE EVALUATION

## A. Simulation Evaluation

The simulation based on PSIM is performed for the proposed inverter. The waveforms of output voltage $V_{o}$, capacitor currents ( $i_{C_{1}}, i_{C_{2}}$ ) and capacitor voltages ( $V_{C 1}, V_{C 2}$ ) are shown in Fig. 10. The following parameters are used for low power simulation. The input voltage is $V_{i n}=12 \mathrm{~V}$, the
module 1 capacitor is $C_{1}=100 \mu \mathrm{~F}$ with $80 \mathrm{~m} \Omega$ ESR, the module 2 capacitor is $C_{2}=220 \mu \mathrm{~F}$ with $50 \mathrm{~m} \Omega$ ESR, the diodes $D_{1}$ and $D_{2}$ have 0.6 V forward voltage drop and $50 \mathrm{~m} \Omega$ internal onstate resistance, and the load resistance is $\mathrm{Ro}=12$ $\Omega$. The $C_{1}=300 \mu \mathrm{~F}$ with $30 \mathrm{~m} \Omega \mathrm{ESR}$, the module 2 capacitor is $C_{2}=560 \mu \mathrm{~F}$ with $20 \mathrm{~m} \Omega \mathrm{ESR}$, and the load resistance is $\mathrm{Ro}=12 \Omega$. The output frequency fs is 25 kHz . The waveforms of low power and high power are demonstrated in Fig. 10(a) and (b), respectively. It can be seen that the proposed inverter can work at higher power. $C_{1}$ and $C_{2}$ can be converted to resonant switchedcapacitor topology easily [29], [30] and hence the less power loss can be achieved in the frontend SC stage.


Fig. 11. Simulation waveforms of 9 -level and 25level inverter, output frequency fs $=25 \mathrm{kHz}$. (a) Output voltage of nine-level inverter ( $k_{1}=k_{2}=$ $0.5, x_{1}=\pi / 8, x_{2}=\pi / 4$ ). (b) Spectrum of nine-level output. (c) Output voltage of 25 -level inverter (same duration of each voltage level). (d) Spectrum of 25-level output.
The simulation waveforms are accorded with theoretical analysis. $C_{1}$ is discharged at the interval of $t_{4}$ to $t_{5}$, and $C_{2}$ is discharged at the interval of $t_{3}$ to $t_{6}$. Both capacitors are charged and discharged once every half cycle. Because of the internal resistance of diodes $D_{1}$ and $D_{2}$, the charging current can be divided into several subintervals that are in accordance with operational analysis in Fig. 4. Considering the charging cycle and RC time constant, the peak current of charging period and voltage drop of
discharging period are rational at the given conditions. Theoretically, low power can obtain amplitude of $\pm 4 \times 12 \mathrm{~V}$, and high power can obtain amplitude of $\pm 4 \times 100 \mathrm{~V}$. However, an amplitude difference emerges between theoretical results and simulation waveforms. In low power simulation, the voltage of the capacitors $C_{1}$ varies between 11 and 11.3 V , while the voltage of the capacitors $C_{2}$ varies between 10.8 and 11.1 V . In high power simulation, the voltage of the capacitors $C_{1}$ varies between 91 and 95 V , while the voltage of the capacitors $C_{2}$ varies between 89 and 91 V . Thus, the amplitude of simulation waveform is less than the theoretical amplitude caused by forward voltage drop and inner resistance. The output voltage and voltage spectrum are compared in Fig. 11, including 9- and 25 -level inverter. Fig. 11(a) is output waveform of nine-level inverter at condition of $k_{1}=k_{2}=0.5, x_{1}=\pi / 8, x_{2}=\pi / 4$. The voltage step in staircase output has a slightly drop at $\mathrm{t}=0.00465-0.00475$ due to the discharging cycle of SC. Fig. 11(c) is output waveform of 25level inverter with the same duration of each voltage level. A thirteen-level inverter adopts $3 \times$ 2 structure, and the following circuit parameters are used. The input voltage is $V_{\text {in }}=12 \mathrm{~V}$, the module 1 capacitors are $C_{1}=100 \mu \mathrm{~F} C_{1}=120 \mu \mathrm{~F}$ with $80 \mathrm{~m} \Omega \mathrm{ESR}$, the module 2 capacitor are $C_{2}=$ $220 \mu \mathrm{~F} C_{2}=250 \mu \mathrm{~F}$ with $50 \mathrm{~m} \Omega \mathrm{ESR}$, and the load resistance is $\mathrm{Ro}=12 \Omega$.

TABLEIV
COMPARISION OF 9 AND 25-LEVEL MULTILEVEL INVERTERS

| Harmonic | 9-level | 25 -level |
| :---: | :---: | :---: |
| Fundamental <br> 1 | 38.8 V | 55.1 V |
| 3 | 6.8 V | 7.2 V |
| 5 | 2.6 V | 2.1 V |
| 7 | 1 V | 2 V |
| 9 | 1 V | 0.5 V |
| THD(\%) | 19.1 | 10.58 |

It can be found from Fig. 11(c) that the voltage drop is indistinctive in each step of staircase
output because the discharging periods of SCs become shorter for $25-l e v e l$ inverter.


Fig.11(e) Output for 9-level


Fig.11(f) Output for 25-level
The output spectrums of 9 -level and 25 -level inverter are illustrated in Fig. 11(e) and (f), respectively. The fundamental frequency is 25 kHz that is the same as output frequency. It can be observed that the fundamental harmonic is significantly higher than the other harmonics. The magnitude of fundamental component is below 40 V for nine-level inverter, while the magnitude of fundamental component is 55 V for a $25-l e v e l ~ i n v e r t e r . ~ T h e ~ d o m i n a t i n g ~ h a r m o n i c s ~$ are compared in Table IV. The calculated THD is $19.1 \%$ for 9 -level inverter and $14.1 \%$ for $25-$ level
 harmonics than nine-level inverter. It can be estimated that the harmonics can be further cut down along with the increasing number of voltage levels. Thus, the proposed inverter produces near sinusoidal staircase output, and two methods can make it more sinusoidal. One is to optimize the duration of voltage levels; the other one is to increase the number of voltage levels.
B. Experimental Evaluation

An experimental prototype was implemented with output frequency of 25 kHz and output power of 50 W . The schematic of modulation circuit is shown in Fig. 12 that is made up of DFF, RSFF, NOT, and XOR. LM393 is a dual comparator operated at single voltage mode. The LOCMOS logic components consisting of HEF4013 (dual D flip-flop), HEF4070 (Quad 2input XOR), HEF4081 (Quad 2-input AND gate), and HEF4069 (Hex Inverters) accomplish the symmetrical PSM. 5 V output in CMOS logic is magnified by boot-strap IC IR2113 to drive power switches. The schematic of power circuit is same as shown in Fig. 1. The switching devices are IRF540 MOSFETs with about $50 \mathrm{~m} \Omega$ on-state resistances. Capacitor $C_{1}$ is $100 \mu \mathrm{~F}$ electrolytic capacitor with ESR $80 \mathrm{~m} \Omega$, while $C_{2}$ is $220 \mu \mathrm{~F}$ electrolytic capacitor with ESR $50 \mathrm{~m} \Omega . V_{\text {in }}$ is 12 V supplied by dc power supply KIKUSUI PAS409. The switching frequency of H -bridge backend is 25 kHz , while the switching frequency of SC frontend is 50 kHz . Ro is $12 \Omega$ resistive load.


Fig. 12. Modulation circuit Schematic diagram Fig. 13 shows the observed waveforms of gate drivers $\left(g_{s_{1}}, g_{s_{1 a}}\right)$, input currents $\left(I_{i n_{1}}, I_{i n_{2}}\right)$, and output voltage $\left(V_{o}\right)$. The switching frequency of $S_{1}, S_{1}^{\prime}, S_{2}$, and $S_{2}^{\prime}$ is twice the output frequency, and the switching frequency of $S_{1 a}-$ $S_{1 d}$ and $S_{2 a}-S_{2 d}$ is the same as the output frequency. Thus, the switching frequency is so
much less than that in multicarrier modulation. $I_{i n_{2}}$ is greater than $I_{i n_{1}}$, so $V_{d c 2}$ provides more11


Fig. 13. Observed waveforms of output voltage, gate drivers, input currents with 25 kHz frequency and $12 \Omega$ load ( $k_{1}=k_{2}=0.5, x_{1}=\pi / 8$, $x_{2}=\pi / 4$ ).
(a) Upper trace: output voltage $V_{o}$; second trace: $S_{1}$ gate driver $g_{s_{1}}$; third trace: $S_{1 a}$ gate driver of $g_{s_{1 a}}$; lower trace: input current $I_{i n_{1}}$.
(b) Upper trace: output voltage $V_{o}$; second trace: $S_{2}$ gate driver $g_{s_{2}}$; third trace: $S_{2 a}$ gate driver $g_{s_{2 a}}$; lower trace: input current $I_{i n_{2}}$.
Fig. 14. Observed waveforms of output voltage, capacitor currents and capacitor voltages with 25 kHz output frequency, and $12 \Omega$ load ( $k_{1}=k_{2}=$ $0.5, x_{1}=\pi / 8, x_{2}=\pi / 4$ ).
(a) Upper trace: output voltage $V_{o}$; middle trace: capacitor current $i_{C_{1}}$; lower trace: capacitor voltage $V_{c 1}$.
(b) Upper trace: output voltage $V_{o}$; middle trace: capacitor current $i_{C_{2}}$; lower trace: capacitor voltage $V_{c 2}$ energy than $V_{d c 1}$.
There is an energy unbalance in each cell with cascaded connection, and the further study is required for power balance. THD of output voltage is $19.7 \%$ for nine-level inverter, which is close to simulation results and theoretical analysis. Fig. 14 shows the observed waveforms of output voltage ( $V_{o}$ ), capacitor currents ( $i_{C_{1}}, i_{C_{2}}$ ), and capacitor voltages ( $V_{c 1}, V_{c 2}$ ).


Fig. 15. Observed output and capacitor voltage at condition of $k_{1}=k_{2}=0.5, x_{1}=\pi / 8, x_{2}=\pi / 4$, and $12 \Omega$ load. (a) Output waveforms of 25 kHz frequency. Upper trace: output voltage $V_{o}$; lower trace: capacitor voltage $V_{C 1}$. (b) Output waveforms of 500 Hz frequency. Upper trace: output voltage $V_{o}$; lower trace: capacitor voltage $V_{C 1}$.
Fig. 16. Output waveforms after LC filter and conversion efficiency. (a) Upper trace: staircase output $V_{o}$; middle trace: output voltage after LC filter $V_{o f}$; lower trace:output current after LC filter $i_{o f}$. (b) Conversion efficiency comparisons of nine-level inverter with 25 kHz output under the condition of $k_{1}=k_{2}=0.5, x_{1}=\pi / 8, x_{2}=\pi / 4$. The observed amplitude of output voltage is lower than the theoretical amplitude 48 V caused by the voltage drop from the internal resistance of MOSFETs, diode, and capacitor.


The charging cycle is divided into several subintervals, and capacitor $C_{1}$ has a shorter discharging cycle than capacitor $C_{2}$. The capacitor voltages $V_{C 1}$ and , $V_{C 2}$ alternatively increase and drop along with charging and discharging operations, respectively. vc1 has the lower ripple voltage than, $V_{C 2}$ due to the shorter discharging period. The experimental results are in accord with the simulation waveforms as
shown in Fig. 10. Fig. 15 shows the observed waveforms at the different output frequencies with the operational condition of $k_{1}=k_{2}=0.5, x_{1}$ $=\pi / 8, x_{2}=\pi / 4$. The same circuit parameters are adopted for comparisons of 25 kHz and 500 Hz . The output and capacitor voltage are demonstrated in Fig. 15(a) with the output frequency of 25 kHz ; the output and capacitor voltage are demonstrated in Fig. 15(b) with the

output frequency of 500 Hz . It can be found that the voltage drop is indistinct in each step of 25 kHz staircase output caused by a shorter discharging cycle. However, a larger voltage drop occurs in each step of 500 Hz staircase output due to a longer discharging cycle. Likewise, the larger ripple can be found in capacitor voltage vc1 with output frequency of 500 Hz . A small LC filter is added in front of resistive load to improve the output harmonics. The filter inductor and capacitor are $50 \mu \mathrm{H}$ and $0.5 \mu \mathrm{~F}$, respectively. Output voltage and current after filter are $V_{\text {of }}$ and $i_{o f}$, both of which are demonstrated in Fig. 16(a). It can be found that the LC filter smoothes the staircase output and more sinusoidal output is obtained for power distribution. The efficiency curves of the simulation and experiment are illustrated in Fig. 16(b). Both simulation and experiment adopt the same circuit parameters with the output frequency of 25 kHz . There are some small differences existed between the results of simulation and experiment due to the discrepancy between the simulation model and the experimental prototype. However, the curvature varied with the output current is almost similar. The main power losses contain switching losses, conduction losses of the
switches, conduction losses of capacitors, and ripple losses of capacitors. It can be found that the proposed inverter can achieve more than $83 \%$ conversion efficiency over a wide range of output current. Meanwhile, total efficiency slightly falls off along with the increase in the output power. The root cause is the increase of conduction losses due to on-resistance of the power MOSFET. With the same circuit parameters, the smooth output is seen in high-frequency scenario. Meanwhile, the capacitor cost of high-frequency scenario can be significantly saved compared with low frequency counterpart. Thus, the proposed modulation and topology are more suitable for high-frequency applications. Furthermore, the charging and discharging frequencies of SCs are twice the output frequency, which is significantly less than the charging and discharging frequencies in multicarrier pulse width modulation [18]. Thus, the capacitor lifetime is prolonged by the reduced times of charging and discharging. Meanwhile, the system reliability is increased due to the same circuit cell and modulation strategy. It is concluded from simulation and experiment that the proposed multilevel inverter and symmetrical modulation are an effective approach to serve as highfrequency power source with higher conversion efficiency.

## VI. CONCLUSION

In this paper, a novel SC-based cascaded multilevel inverter was proposed. Both 9-level and 25 -level circuit topology are examined in depth. Compared with conventional cascaded multilevel inverter, the proposed inverter can greatly reduces the number of switching devices. A single carrier modulation called by symmetrical PSM, was presented with the low switching frequency and simple implementation. The accordant results of simulation and experiment further confirm the feasibility of proposed circuit and modulation method.

Comparing with traditional cascade H -bridge, the number of voltage levels can be further increased by SC frontend. For instance, the number of voltage levels increases twice in half cycle of 9level circuit, and the number of voltage levels increases three times in half cycle of 25 -level circuit. With the exponential increase in the number of voltage levels, the harmonics are significantly cut down in staircase output, which is particularly remarkable due to simple and flexible circuit topology. Meanwhile, the magnitude control can be accomplished by pulsewidth regulation of voltage level, so the proposed multilevel inverter can serve as HF power source with controlled magnitude and fewer harmonics. This paper mainly analyses the nine-level and $25-l e v e l$ inverters. The method of analysis and design is also applicable to other members of the proposed inverter. The proposed inverter can be applied to grid-connected photovoltaic system and electrical network of EV, because the multiple dc sources are available easily from solar panel, batteries, ultracapacitors, and fuel cells.

## VII.REFERENCES

[1]. Junfeng Liu ,K. W. E. Cheng, Senior member ,IEEE , and Yuanmao Ye "A Cascaded Multi level Inverter Based On switched Capacitor for High frequency AC power distribution system ,"IEEE Transactions on power electronics,vol..,29,n0.8 August 2020. P. Jain and H. Pinheiro, "Hybrid high frequency AC power distribution architecture for telecommunication systems," EEE Trans. Aerospace Electron. Syst., vol. 35, no. 1, pp. 138-147, Jan. 1999.
[2]. J. Drobnik, "High frequency alternating current power distribution," in Proc. 16th Int.Telecommun. Energy Conf., (INTELEC ‘94), Oct. 30-Nov. 3, pp. 292-296.
[3]. B. K. Bose, M.-H. Kin, and M. D. Kankam, "High frequency AC vs. DC distribution system for next generation hybrid electric vehicle," in Proc. IEEE Int. Conf. Ind. Electron., Control, Instrum. (IECON), Aug. 5-10, 1996, vol. 2, pp. 706-712.
[4]. S. Chakraborty and M. G. Simoes, "Experimental evaluation of active filtering in a single-phase high-frequency AC microgrid," IEEE Trans. Energy Convers., vol. 24, no. 3, pp. 673-682, Sep. 2009.
[5]. R. Strzelecki and G. Benysek, Power Electronics in Smart Electrical Energy Networks. London, U.K.: Springer-Verlag, 2008.
[6]. Z. Ye, P. K. Jain, and P. C. Sen, "A two-stage resonant inverter with control of the phase angle and magnitude of the output voltage," IEEE Trans. Ind. Electron., vol. 54, no. 5, pp. 2797-2812, Oct. 2007.
[7]. L. M. Tolbert, F. Z. Peng, and T. G. Habetler, "Multilevel PWM methods at low modulation indices," IEEE Trans. Power Electron., vol. 15, no. 4, pp. 719-725, Jul. 2000.
[8]. C. C. Antaloae, J. Marco, and N. D. Vaughan, "Feasibility of high frequency alternating current power for motor auxiliary loads in vehicles," IEEE Trans. Veh. Technol., vol. 60, no. 2, pp. 390-405, Feb. 2011.
[9]. K. W. E. Cheng, "Computation of the AC resistance of multistranded conductor inductors with multilayers for high frequency switching converters," EEE Trans. Magn., vol. 36, no. 4, pp. 831-834, Jul. 2000.
[10]. P. P. Rodriguez, M. M. D. Bellar, R. R. S. Munoz-Aguilar, S. S. Busquets- ~ Monge, and F. F. Blaabjerg, "Multilevel clamped multilevel converters (MLC)," IEEE Trans. Power Electron., vol. 27, no. 3, pp. 1055-1060, Mar. 2012.
[11]. K. Ilves, A. Antonopoulos, S. Norrga, and H.-.P. Nee, "A new modulation method for the modular multilevel converter allowing
fundamental switching frequency," IEEE Trans. Power Electron., vol. 27, no. 8, pp. 3482-3494, Aug. 2012.
[12]. H. Akagi, "Classification, terminology, and application of the modular multilevel cascade converter (MMCC)," IEEE Trans. Power Electron., vol. 26, no. 11, pp. 3119-3130, Nov. 2011.
[13]. M. F. Kangarlu and E. Babaei, "A generalized cascaded multilevel inverter using series connection of sub multilevel inverters," $\operatorname{EEEE}$ Trans. Power Electron., vol. 28, no. 2, pp. 625636, Feb. 2013.
[14]. H. L. Chan, K. W. E. Cheng, and D. Sutanto, "Bidirectional phase-shifted DC-DC converter," IEEE Electron. Lett., vol. 35, no. 7, pp. 523-524, Apr. 1999.
[15]. O.-C. Mak and A. Ioinovici, "Switchedcapacitor inverter with high power density and enhanced regulation capability," IEEE Trans. Circuits Syst. I: Fundam. Theory Appl., vol. 45, no. 4, pp. 336-347, Apr. 1998.
[16]. S.-J. Park, F.-S. Kang, M. H. Lee, and C.-U. Kim, "A new single-phase five-level PWM inverter employing a deadbeat control scheme," $\operatorname{EEE}$ Trans. Power Electron., vol. 18, no. 3, pp. 831843, May 2003.
[17]. B. Axelrod, Y. Berkovich, and A. Ioinovici, "A cascade boost-switched capacitor-converterTwo level inverter with an optimized multilevel output waveform," IEEE Trans. Circuits Syst. I: Reg. Papers, vol. 52, no. 12, pp. 2763-2770, Dec. 2005.
[18]. Y. Hinago and H. Koizumi, "A single-phase multilevel inverter using switched series/parallel DC voltage sources," IEEE Trans. Ind. Electron., vol. 57, no. 8, pp. 2643-2650, Aug. 2010.
[19]. Y. Hinago and H. Koizumi, "A switchedcapacitor inverter using series/parallel conversion with inductive load," IEEE Trans.

Ind. Electron., vol. 59, no. 2, pp. 878-887, Feb. 2012.
[20]. M. S. W. Chan and K. T. Chau, "A new switched-capacitor boost multi level inverter using partial charging," IEEE Trans. Circuits Syst. II: Exp. Briefs, vol. 54, no. 12, pp. 11451149, Dec. 2007.
[21]. K. K. Law and K. W. E. Cheng, "Examination of the frequency modulation and lifting techniques for the generalized power factor correction switched-capacitor resonant converter," Int. J. Circuit Theory Appl., vol. 36, no. 7, pp. 839855, Oct. 2008.
[22]. A. K. Gupta and A. M. Khambadkone, "A space vector modulation scheme to reduce common mode voltage for cascaded multilevel inverters," IEEE Trans. Power Electron., vol. 22, no. 5, pp. 1672-1681, Sep. 2007.
[23]. S. Kouro, P. Lezana, M. Angulo, and J. Rodriguez, "Multicarrier PWM with DC-link ripple feedforward compensation for multilevel inverters," IEEE Trans. Power Electron., vol. 23, no. 1, pp. 52-59, Jan. 2008.
[24]. D. Zhong, L M. Tolbert, and J. N. Chiasson, "Active harmonic elimination for multilevel converters," IEEE Trans. Power Electron., vol. 21, no. 2, pp. 459-469, Mar. 2006.
[25]. A. Kavousi, B. Vahidi, R. Salehi, M. Bakhshizadeh, N. Farokhnia, and S. S. Fathi, "Application of the Bee algorithm for selective harmonic elimination strategy in multilevel inverters," IEEE Trans. Power Electron., vol. 27, no. 4, pp. 1689-1696, Apr. 2012.
[26]. K. Ding, K. W. E. Cheng, and Y. P. Zou, "Analysis of an asymmetric modulation method for cascaded multilevel inverters," IET Power Electron., vol. 5, no. 1, pp. 74-85, Jan. 2012.
[27]. Y. Zhongming, P. K. Jain, and P. C. Sen, "A fullbridge resonant inverter with modified phaseshift modulation for high-frequency AC power distribution systems," IEEE Trans. Ind.

Electron., vol. 54, no. 5, pp. 2831-2845, Oct. 2007.
[28]. A. Ioinovici, "Switched-capacitor power electronics circuits," IEEE Circuits Syst. Mag., vol. 1, no. 1, pp. 37-42, Jan. 2001.
[29]. K. K. Law, K. W. E. Cheng, and Y. P. B. Yeung, "Design and analysis of switched-capacitor based step-up resonant converters," IEEE Trans. Circuit Syst. I, Reg. Papers, vol. 52, no. 4, pp. 943-948, Apr. 2005.
[30]. Y. Yuanmao and K. W. E. Cheng, "A family of single-stage switched capacitor-inductor PWM converters," IEEE Trans. Power Electron., vol. 28, no. 11, pp. 5196-5205, Nov. 2013.
[31]. P. Jain and H. Pinheiro, "Hybrid high frequency AC power distribution architecture for telecommunication systems," EEE Trans. Aerospace Electron. Syst., vol. 35, no. 1, pp. 138-147, Jan. 1999.

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