

Design Synthesis of a Microstripline Coupler

Akansha Kumari¹, Dr. K. B. Singh², Dr. Pankaj Kumar³

¹Research Scholar, University Department of Electronics, B. R. A. Bihar University, Muzaffarpur, Bihar, India

² & ³P. G. Department of Physics, L. S. College, Muzaffarpur, B. R. A. Bihar University, Muzaffarpur, Bihar, India

E-mail : kbsaku@gmail.com

ABSTRACT

Several authors have developed various methods for the study of characteristics of single & coupled microstriplines. This paper deals with the analytical studies of the design synthesis of microstripline couplers and their variation with geometry and frequency using Alumina substrates for the design synthesis of the microstripline coupler which is the aim of the present work. All the parallel line couplers, whether mode of propagation is true TEM or not, have the even and odd-mode property which always results in even- mode characteristic impedance (Z_{oe}) and odd-mode characteristic impedance (Z_{oo}).

Keywords : Microstripline, Couplers, Antenna, Characteristics Impedance.

Article Info

Volume 9, Issue 4

Page Number : 624-628

Publication Issue

July-August 2022

Article History

Accepted : 10 August 2022

Published : 28 August 2022

I. INTRODUCTION

For the study of the characteristic impedance of the microstripline coupler we develop the mathematical formula for even and odd-mode and then we will calculate the results. With the help of these results design synthesis technique is used to obtain the geometrical parameters of a coupler of given parameters. The mathematical formulation is based on the conformal transformation technique developed by H.A. Wheeler and Calculation is based on the computer programming developed by S. K. Kaul using closed form formula of Schwarzmann. This technique is too much popular now-a-days and provides an easy approach for the analysis and synthesis of single and coupled microstriplines and other structures useful in MIC's.

II. METHODS AND MATERIAL

Parallel plate striplines support pure TEM mode of propagation but microstrip cannot support pure TEM mode as it is an inhomogeneous structure and it supports quasi-TEM mode [1-5]. However, at low frequency the mode of propagation closely resembles the TEM mode. Wheeler calculated capacitances, phase velocities and impedances of single and coupled strips. Following these various approximate methods have been adopted by Crystal, H. Howe, MAR Gunston, Policky and Stover etc. Bryant and Weis used Green's function technique and calculated the even- and odd- mode impedances of the coupled microstrip lines. S. Akhtarzad, Thomas R. Rowbotham and Peter B. Johns, M.K. Krage and G.I. Haddad also calculated the even- and odd- mode characteristic impedances of coupled microstrip using

different techniques. E. Yamashita and R. Mitra presented an analysis based on variation principle. These results were found in reasonable agreement amongst themselves. Banmali, Rawat and Babu using methods of images calculated the characteristic parameters and founded them in close agreement with each other. The results obtained by image method were intermediate between Wheeler’s two results for wide and narrow strips [6-10].

This leads to very useful design criteria especially at lower frequencies. The quasi-TEM allows the magnetic and electric fields to be considered, separately. When only the magnetic field is considered, the dielectric inhomogeneity is ignored, since the dielectric medium is treated as free space. But when considering the electric field, the inhomogeneity must be taken into account since the normal component of electric field is discontinuous at the dielectric interface.

The present paper involves the problems in quasi-static limit in lower giga hertz range of frequency.

III. RESULTS AND DISCUSSION

1.1 Formulation of the problem for even and odd-modes characteristic impedances of a microstripline coupler

The study of microstripline coupler involves the analysis of even- and odd- modes of propagation. In the even-mode, energy traveling down, one microstrip line is coupled into a parallel line and travels in the same direction, where as in the odd-mode energy travels in the reverse direction after coupling.

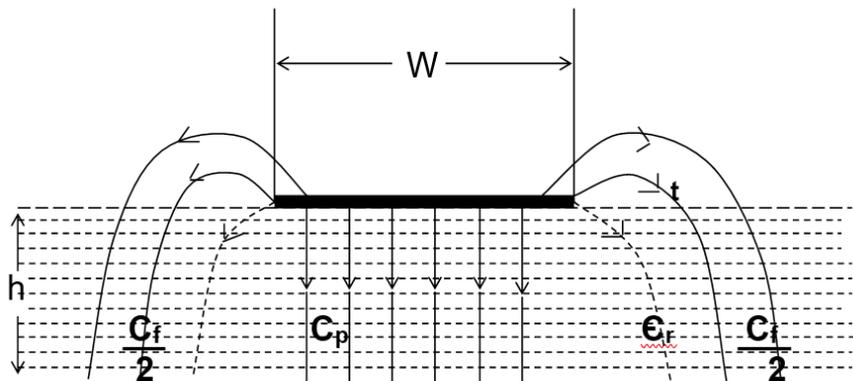


Fig.1: Electric field configuration in a microstrip (Isolated)

$$Z = \frac{n\sqrt{\epsilon_{re}}}{\frac{1}{w/h + 2w/3h\sqrt{\epsilon_{re}} + 2.7/\log 4h/t}}$$

Where, $n=377\Omega$ = free space impedance, w = strip width, h = substrate height, t = strip thickness, and ϵ_{re} = effective relative permittivity.

The derivation of the equation for the modes begins with the consideration of a basic single microstrip conductor shown in Fig (1). The characteristic impedance can be calculated with the help of elementary transmission line equation expressed as [11]

$$Z_o = \frac{1}{V_P C_P} \quad \text{-----} \quad 1$$

Where, V_P = phase velocity of the wave traveling along the microstrip line.

C_P = capacitance per unit length of the line.

The capacitance of the line is the result of the combination of different components indicated in fig (1). These are:

C_{PP} = parallel plate capacitance between lower surface of the microstrip and the ground plane and is given by

$$C_{PP} = [\epsilon_{\text{reff}}/c.\eta]. (w/h) \quad \text{-----} \quad 2$$

C_{PPU} = capacitance between the upper surface of the microstrip and the ground plane which is expressed as

$$C_{PPU} = (2/3) [\epsilon_{\text{reff}}/c.\eta]. (w/h) \quad \text{-----} \quad 3$$

C_F = the fringing capacitance at the edges of the microstrip and is expressed

$$C_F = [\epsilon_{\text{reff}}/ c.\eta]. (2.7/\text{Log}4h/t) \quad \text{-----} \quad 4$$

Where,

- w = microstrip width
- ϵ_{reff} = the effective dielectric constant of the medium
- h = height of the substrate
- η = free space impedance = 377 Ω
- c = the velocity of light in free space
= 3.0 X 10⁸ m/sec.
- t = microstrip thickness.

Thus, the total capacitance (C_P) of the isolated microstrip structure is expressed as

$$C_P = C_{PP} + C_{PPU} + C_F$$

or $C_P = (\epsilon_{\text{reff}} / c.\eta) (w/h) + (2/3) (\epsilon_{\text{reff}} / c.\eta) (w/h) (\epsilon_{\text{reff}} / c.\eta). (2.7/\text{Log}4h/t)$

5

This is the expression of the capacitance of the microstrip structure in terms of its geometric parameters.

The phase velocity V_P can be calculated by the formula

$$V_P = c / \epsilon_{\text{reff}} \quad \text{-----} \quad 6$$

For wide strip, ϵ_{reff} , ϵ_r , and

For narrow strip, ϵ_{reff} $(\epsilon_r + 1) / 2$

Where,

ϵ_r = relative dielectric constant.

From equations 1, 5, and 6, we get

$$Z_o = (\epsilon/\epsilon_{\text{reff}}). [1/[(w/h) + (2w/3h) + (2.7/\text{Log}4h/t)]] \quad \text{-----} \quad 7$$

The calculations made on the basis of this expression give the characteristics impedance, the propagation constant and other transmission parameters of a single microstrip structure.

When the second conductor is introduced close to the first one, the field distribution gets altered. In even-mode the electric field lines follow the pattern fairly similar to that of the isolated conductor. In case of odd-mode, the two conductors are linked by the electric field lines.

The form of equation 6 obtained for the isolated microstrip line are also useful in calculating the characteristic impedance of microstrip coupler in even- and odd- modes. In the even-mode C_p is replaced by C_{PO} and in the odd-mode by C_{PO} . Since the electric field lines are distributed in air and below the conductor in the dielectric substrate, the dielectric medium now becomes inhomogeneous. Due to inhomogeneity the phase velocity (V_p) for the isolated case is replaced by V_{PO} for the even- mode and V_{PO} for the odd- mode. Further in place of ϵ_{reff} the effective dielectric constants $(\epsilon_{\text{reff}})_e$ and $(\epsilon_{\text{reff}})_o$ are to be used for even- and odd- modes separately. Similarly Z_{oe} and Z_{oo} represent the characteristic impedances for even-and odd- modes respectively.

3.2. Even mode characteristics impedance (Z_{oe})

The total capacitance is constituted by the following components:

C_{PPE} = parallel plate capacitance as equation 4.2.2 for even mode.

C_{PPU} = capacitance between upper surface of the conductor and ground plane as equation (4.2.3)

C'_{PPU} = capacitance between strip conductor and ground plane enclosed between two striplines.

$$= (2\epsilon_{\text{reff}} / 3 c.\eta). (w/h). (1/ [(w/s) + 1]) \quad \text{-----} \quad 8$$

C_F = Fringe capacitance at the edge of the striplines as equation 4.

C'_F = Fringe capacitance between two edges of the microstripline.

$$= (\epsilon_r / c.\eta) (2.7/\log(4h/t)) . (1/[(w/s) + 1]) \quad \text{-----} \quad 9$$

Thus the total capacitance for even-mode coupled lines is expressed as

$$C_{PE} = C_{PPE} + (1/2)C_{PPU} + (1/2)C_F + (1/2)C'_{PPU} + (1/2)C'_F \quad \text{-----} \quad 10$$

Now we can write the characteristic impedance for even-mode configuration as

$$Z_{oe} = (\eta / \sqrt{\epsilon_{\text{reff}}}). [1/ [(w/h) + (w/3h) + (1.35/\log(4h/t)) + (w/3h).(1/((w/s)+1)) + (1.35/\log(4h/t)). (1/ ((w/s) + 1))]] \quad \text{-----} \quad 11$$

and for $t = 0$

$$Z_{oe} = (\eta / \sqrt{\epsilon_{\text{reff}}}). [1/ \{(w/h) [1 + (1/3\sqrt{\epsilon_{\text{reff}}})] + (1/3\sqrt{\epsilon_{\text{reff}}}). (w/h) (1/ (w/s) + 1)\}] \\ = (\eta / \sqrt{\epsilon_{\text{reff}}}). [1/ \{(w/h) [1 + (1/3\sqrt{\epsilon_{\text{reff}}})] + (1/3\sqrt{\epsilon_{\text{reff}}}) (1/(w/s)+1)\}] \quad \text{----} \quad 12$$

3.3 Odd-mode characteristic impedance (Z_{oo})

In the case of odd- mode coupled lines, the total capacitance (C_{PO}) is determined in terms of the following components:

C''_{PPU} = capacitance between strip conductor and the ground plane spaces enclosed between the two microstrip lines.

$$= (8/3). (\epsilon_{\text{reff}} / c.\eta) \quad \text{-----} \quad 13$$

C''_F = Fringe capacitance between edges of the microstrip lines and is given as

$$= (\epsilon_{\text{reff}} / c.\eta) [2.7 / \log (4\text{stan} (4h/s)/ t)] \quad \text{-----} \quad 14$$

The total capacitance of the odd-mode coupled lines is thus expressed as

$$C_{PO} = C_{PP} + (1/2)C_{PPU} + (1/2)C''_{PPU} + (1/2)C_F + (1/2)C''_F \quad \text{-----} \quad 15$$

And the odd-mode characteristic impedance (Z_{oo}) is given as

$$Z_{oo} = (\eta / \epsilon_{\text{reff}}). [1/ \{(w/h) + (w/3h\epsilon_{\text{reff}}) + (1.35/\log(4h/t))(4/3\epsilon_{\text{reff}}).(1/((s/w)+1)) + (1.35/\log(4\text{stan} (4h/s)/ t))\}] \quad \text{-----} \quad 16$$

When, $t = 0$

$$Z_{oo} = (\eta / \epsilon_{\text{reff}}). [1/ \{(w/h) [1 + (1/3\epsilon_{\text{reff}}) + (4/3\epsilon_{\text{reff}}) (1/(s/w) + 1)\}] \quad \text{---} \quad 17$$

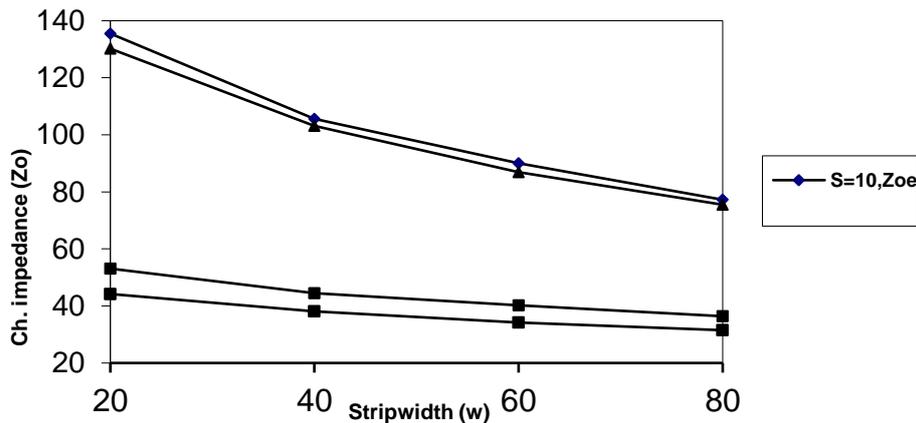
Table – 1: Dependence of characteristic impedance of coupled microstripline for even & odd-modes on strip width

h = 100 mils, t = 0.01 mils, f = 2 GHz, $\epsilon_r = 9.6$,
 1 mils = 10^{-3} inch = 2.54 μm

Stripwidth	S=10mils				S=20mils			
W (mils)	Z_{oe} Ω	Z_{oo} Ω	$(\epsilon_{\text{reff}})_e$	$(\epsilon_{\text{reff}})_o$	Z_{oe} Ω	Z_{oo} Ω	$(\epsilon_{\text{reff}})_e$	$(\epsilon_{\text{reff}})_o$
20	135.50	44.20	6.52	5.42	130.20	53.10	6.65	5.40
40	105.60	38.12	6.80	5.40	103.12	44.50	6.92	5.35
60	90.10	34.20	7.12	5.39	86.90	40.20	7.15	5.32
80	77.25	31.50	7.28	5.35	75.50	36.40	7.35	5.28

Graph – 1: Dependence of characteristic impedance of coupled microstripline for even & odd-modes on strip width

h = 100 mils, t = 0.01 mils, f = 2 GHz, $\epsilon_r = 9.6$
 1 mils = 10^{-3} inch = 2.54 μm



3.4 Design synthesis of microstripline coupler

The coupling coefficient (C) at mid band frequency has been expressed in equation 17. The feed line characteristic impedance is given by

$$Z_o = [Z_{oe} \times Z_{oo}]^{1/2} \tag{18}$$

Now for the design of a microstripline directional coupler of given coupling coefficient and feed line characteristic impedance we calculate even and odd-modes characteristic impedances using equations

$$Z_{oe} = Z_o [(1 + C) / (1 - C)]^{1/2} \tag{19}$$

$$Z_{oo} = Z_o [(1 - C) / (1 + C)]^{1/2} \tag{20}$$

Again using these values of characteristic impedances shape ratio for Alumina dielectric substrate ($\epsilon_r = 9.6$) is expressed as

$$W/h = 20.37 [4/ Z_{oe} + 1/ Z_{oo}] \tag{21}$$

And approximate value space ratio is given by

$$s/h = 377 (4 Z_{oo} + Z_{oe}) / (3 + 5 \sqrt{\epsilon_r}) Z_o^2 \quad \text{-----} \quad 22$$

Using these equations stripwidth and spacing between two striplines have been calculated for given coupling. Again these values of shape ratio and space ratio are used to calculate Z_{oo} and Z_{oe} and results obtained are compared for conformity as $Z_{oe} = 86.6 \Omega$ and $Z_{oo} = 28.8 \Omega$ for $w = 18.8$ mils and $s = 15$ mils. Here 1 mil stand for 10^{-3} inch.

IV. CONCLUSION

From the study of dependence of characteristic impedance of the microstripline directional coupler for even and odd-modes with strip width, spacing between two striplines and height of the dielectric substrates and also from the study of variation of guide wavelength for even and odd-modes with stripwidth, spacing and height of the substrate we draw useful information for design of directional couplers of different coupling coefficient and feed line characteristic impedance. These results obtained in the synthesis process are also reasonable agreement with those obtained in analysis process. So, this provides an important and necessary tool for the designer to fabricate directional coupler of desired coupling coefficient and directivity. This also provides scope for future work.

V. REFERENCES

- [1]. S. Liao, Microwave device and circuits. PHI. N. Delhi, 1995.
- [2]. K. C. Gupta, Microwave; Wiley Eastern Pvt. Ltd. Publication, 1995.
- [3]. H. Howe, Stripline circuit design of coupled Parallel lines; Artech House, 74, page 112-137
- [4]. H. A. Wheller, Transmission line properties of parallel strip separated by dielectricsheet. IEEE, Tr. MTT-13, 1965.
- [5]. H. A. Wheeler, Transmission line properties of parallel wide strip by conformal mapping approximation. IEEE; MTT vol. 12.
- [6]. B. Bhat and S. K. Koul, Stripline like transmission lines for MIC's; Wiley Eastern Limited, 1990.
- [7]. P. M. T. Ikonen, S.I. Maslovski, C.R. Simovski, and S.A. Tretyakov, on artificial magnetodielectric loading for improving the impedance bandwidth properties of microstrip antennas, IEEE Trans. Antennas Propag. 54, pp.1654–1662. 2006
- [8]. Yoonjae Lee and Yang Hao, "Characterization of microstrip patch antennas on metamaterial Substrates loaded with complementary split-ring Resonators" Wiley Periodicals, Inc. Microwave Opt Technol. Lett. 50, pp.2131–2135, 2008.
- [9]. Welcome to antennas 101" by Louis E. Frenzel, "Electronic Design" 2008
- [10]. Hou, D. B.; et, al., "Elimination of scan blindness with compact defected ground structures in microstrip phased array", IET Microwaves, Antennas and Propagation, 3: 269–275, doi:10.1049/iet-map:20080037, 2009.
- [11]. Guha, D.; Biswas, S.; Antar, Y. "Defected Ground Structure for Microstrip Antennas", in Microstrip and Printed Antennas: New Trends, Techniques, and Applications, John Wiley & Sons: UK, doi:10.1002/9780470973370, 2011.
- [12]. Pozar, David M., Microwave Engineering Addison–Wesley Publishing Company. ISBN 978-81-265-4190-4, 2017.
- [13]. Lee, Kai Fong; Luk, Kwai Man," Microstrip Patch Antennas". World Scientific. pp. 8–12. ISBN 978-9813208612, 2017.
- [14]. Pandey, Anil, "Practical Microstrip and Printed Antenna Design", Bostan: Artech House. p. 443. ISBN 9781630816681, 2019.

Cite this article as :

Akansha Kumari, Dr. K. B. Singh, Dr. Pankaj Kumar, "Design Synthesis of a Microstripline Coupler", International Journal of Scientific Research in Science and Technology (IJSRST), Online ISSN : 2395-602X, Print ISSN : 2395-6011, Volume 9 Issue 4, pp. 624-629, July-August 2022. Available at doi : <https://doi.org/10.32628/IJSRST2294104>
Journal URL : <https://ijsrst.com/IJSRST2294104>